

G.S.C.E.

Solution of 2D

1b

$$\text{Area of the hall} = 3600 * 1500$$

$$\text{Area of each stone} = (60 * 50)$$

$$\text{Therefore, number of stones} = (3600 * 1500 / 60 * 50) = 1800$$

2b

Let, each side = a. Then, original area = a^2 .

$$\text{New side} = 150a/100 = 3a/2. \text{ New area} = 9a^2/4.$$

$$\text{Required ratio} = 9a^2/4 : a^2 = 9:4$$

3a

$$d = 12, r = 6;$$

$$\text{Volume of the largest sphere} = 4/3 \pi r^3$$

$$= 4/3 * \pi * 6 * 6 * 6 = 288\pi \text{ cm}^3$$

4c

$$\text{Area} = \text{Total cost} / \text{Rate} = (1215/135) \text{ hectares} = (9 * 10000) \text{ sq.m.}$$

$$\text{Therefore, side of the square} = \sqrt{90000} = 300\text{m.}$$

$$\text{Perimeter of the field} = (300 * 4)\text{m} = 1200\text{m}$$

$$\text{Cost of fencing} = \text{Rs.}(1200 * 3/4) = \text{Rs.}900$$

5d

$$\text{Required area} = (63 * 63 - 4 * 1/4 * 22/7 * 63/2 * 63/2) = 850.5\text{m}^2$$

6c

$$2\pi r - r = 37 \text{ or } (2\pi - 1)r = 37.$$

$$\text{Or } (2 * 22/7 - 1)r = 37 \text{ or } 37r/7 = 37 \text{ or } r = 7.$$

$$\text{Therefore, Area} = \pi r^2 = (22/7 * 7 * 7) = 154 \text{ cm}^2$$

7b

Let, length= x meters and breadth= y meters

Then $xy=60$ and $\sqrt{x^2+y^2} + x = 5$

Therefore, $x=60$ and $(x^2+y^2) = (5y-x)^2$

Or $xy=60$ and $24y^2-10xy=0$.

Therefore, $24y^2-10*60=0$ or $y^2= 25$ or $y=5$.

Therefore, $x = (60/5)m = 12m$. So, length of the carpet = 12m

8b

Length of wire= circumference of circle of radius 42cm= $(2 * 22/7 * 42) = 264$ cm.

Therefore, perimeter of rectangle= 264 cm.

Let, length= 6x cm & breadth= 5x cm.

Therefore, $2(6x+5x) = 264$ or $x=12$.

Therefore, smaller side= 60 cm

9c

Area= $\sqrt{3/4} * (3\sqrt{3})^2 = 27\sqrt{3/4}$.

Therefore height= $27\sqrt{3/4} * 2/3\sqrt{3} = 9/2 = 4.5$ cm

10c

Distance moved by toothed wheel in 15 revolutions=
 $(15 * 2 * 22/7 * 25)$

Distance moved by smaller wheel in 1 revolution= $(2 * 22/7 * 15)$

Therefore, required number of revolutions= $(15 * 44/7 * 25 * 7 / 44 * 15) = 25$

11b

$1/2 (12+8)d = 840$ or $d = 84$ m

12c

Perimeter= Distance covered in 8 min

$$= (12000/60 * 8)m = 1600m$$

Let, length= $3x$ meters and breadth= $2x$ meters

$$\text{Then, } 2(3x+2x) = 1600 \text{ or } x = 160$$

Therefore, length= 480 m and breadth= 320m

$$\text{Therefore, area} = (480 * 320)m^2 = 153600 m^2$$

13b

Length of the diagonal= Distance covered in 3 min. at 4 km/hr.

$$= (4000/60 * 3) = 200m.$$

Therefore, Area of the field= $\frac{1}{2} * \text{diagonal}^2$

$$= \frac{1}{2} * 200 * 200 = 20000 m^2$$

14C

$$2\pi(R-r) = 60 \Rightarrow 2 * \frac{22}{7} * (R-r) = 60.$$

$$\text{Therefore, } (R-r) = \left(\frac{66 * 7}{44}\right) = 10.5m$$

15b

Let the other sides be x and y . Then,

$$x^2 + y^2 = 13^2 = 169. \text{ Also, } \frac{1}{2} xy = 30 \Rightarrow xy = 60.$$

$$\text{Therefore, } (x+y) = \sqrt{(x^2+y^2)+2xy} = \sqrt{(169+120)} = \sqrt{289} = 17.$$

$$(x-y) = \sqrt{(x^2+y^2)-2xy} = \sqrt{(169-120)} = \sqrt{49} = 7.$$

Solving $x+y=17$, $x-y=7$, we get $x=12$ and $y=5$.

16d

$$360^\circ$$

17B

$$\text{Perimeter} = \text{Distance covered in 8 min.} = \left(\frac{12000}{60} \times 8 \right) \text{m} = 1600 \text{ m.}$$

Let length = $3x$ metres and breadth = $2x$ metres.

$$\text{Then, } 2(3x + 2x) = 1600 \text{ or } x = 160.$$

$$\therefore \text{Length} = 480 \text{ m and Breadth} = 320 \text{ m.}$$

$$\therefore \text{Area} = (480 \times 320) \text{ m}^2 = 153600 \text{ m}^2.$$

18B

$$\frac{2(l + b)}{b} = \frac{5}{1}$$

$$\Rightarrow 2l + 2b = 5b$$

$$\Rightarrow 3b = 2l$$

$$b = \frac{2}{3}l$$

$$\text{Then, Area} = 216 \text{ cm}^2$$

$$\Rightarrow l \times b = 216$$

$$\Rightarrow l \times \frac{2}{3}l = 216$$

$$\Rightarrow l^2 = 324$$

$$\Rightarrow l = 18 \text{ cm.}$$

19B

$$\text{Area of the park} = (60 \times 40) \text{ m}^2 = 2400 \text{ m}^2.$$

$$\text{Area of the lawn} = 2109 \text{ m}^2.$$

$$\therefore \text{Area of the crossroads} = (2400 - 2109) \text{ m}^2 = 291 \text{ m}^2.$$

Let the width of the road be x metres. Then,

$$60x + 40x - x^2 = 291$$

$$\Rightarrow x^2 - 100x + 291 = 0$$

$$\Rightarrow (x - 97)(x - 3) = 0$$

$$\Rightarrow x = 3.$$

20C

$$\begin{aligned}\text{Other side} &= \sqrt{\left(\frac{15}{2}\right)^2 - \left(\frac{9}{2}\right)^2} \text{ ft} \\ &= \sqrt{\frac{225}{4} - \frac{81}{4}} \text{ ft} \\ &= \sqrt{\frac{144}{4}} \text{ ft} \\ &= 6 \text{ ft.}\end{aligned}$$

\therefore Area of closet = (6×4.5) sq. ft = 27 sq. ft.

21D

Let original length = x and original breadth = y .

$$\begin{aligned}\text{Decrease in area} &= xy - \left(\frac{80}{100}x \times \frac{90}{100}y\right) \\ &= \left(xy - \frac{18}{25}xy\right) \\ &= \frac{7}{25}xy.\end{aligned}$$

\therefore Decrease % = $\left(\frac{7}{25}xy \times \frac{1}{xy} \times 100\right)\% = 28\%$.

22B

$$\sqrt{l^2 + b^2} = \sqrt{41}.$$

Also, $lb = 20$.

$$(l + b)^2 = (l^2 + b^2) + 2lb = 41 + 40 = 81$$

$$\Rightarrow (l + b) = 9.$$

\therefore Perimeter = $2(l + b) = 18$ cm.

23B

Let original length = x and original breadth = y .

Original area = xy .

New length = $\frac{x}{2}$.

New breadth = $3y$.

New area = $\left(\frac{x}{2} \times 3y\right) = \frac{3}{2}xy$.

\therefore Increase % = $\left(\frac{1}{2}xy \times \frac{1}{xy} \times 100\right)\% = 50\%$.

24D

We have: $l = 20$ ft and $lb = 680$ sq. ft.

So, $b = 34$ ft.

\therefore Length of fencing = $(l + 2b) = (20 + 68)$ ft = 88 ft.

25C

$$\begin{aligned}\text{Area to be plastered} &= [2(l + b) \times h] + (l \times b) \\ &= \{[2(25 + 12) \times 6] + (25 \times 12)\} \text{ m}^2 \\ &= (444 + 300) \text{ m}^2 \\ &= 744 \text{ m}^2.\end{aligned}$$

\therefore Cost of plastering = Rs. $\left(744 \times \frac{75}{100}\right) = \text{Rs. } 558$.